

Basic details

|  |  |                 |                            |                          |
|--|--|-----------------|----------------------------|--------------------------|
| UID  | <input type="text"/>   | Cohorts covered | Earliest cohort<br>2019-20 | Latest cohort<br>2019-20 |
| Long title   | Mathematical Analysis  |                 |                            |                          |
| New code   | PHYS40007  | New short title | Mathematical Analysis      |                          |
| Brief description of module<br><i>(approx. 600 chars.)</i> | <p>This module is intended to help students to think “like a mathematician” and to understand the mathematics underlying notions of limits and infinity with particular emphasis on the underpinnings of Calculus. Examples of physical contexts such as approximations using the Taylor series will illustrate the importance of these ideas in physics. Time will also be devoted to developing the ability to write rigorous proofs in these contexts.</p> <p style="text-align: right;">438 characters</p> |                 |                            |                          |
| Available as a standalone module/ short course?            | N  |                 |                            |                          |

Statutory details

|              |           |            |                 |             |                      |
|--------------|-----------|------------|-----------------|-------------|----------------------|
| Credit value | ECTS<br>5 | CATS<br>10 | Non-credit<br>N | HECOS codes | <input type="text"/> |
| FHEQ level   | 4         |            |                 |             | <input type="text"/> |

Allocation of study hours

|                   | Hours |   |
|-------------------|-------|---|
| Lectures          | 27    |   |
| Group teaching    | 6     | <i>Incl. seminars, tutorials, problem classes.</i>  |
| Lab/ practical    | 0     |   |
| Other scheduled   | 12    | <i>Incl. project supervision, fieldwork, external visits.</i>                               |
| Independent study | 80    | <i>Incl. wider reading/ practice, follow-up work, completion of assessments, revisions.</i> |
| Placement         | 0     | <i>Incl. work-based learning and study that occurs overseas.</i>                            |
| Total hours       | 125   |   |
| ECTS ratio        | 25.00 |   |

Project/placement activity

Is placement activity allowed?

Module delivery

|               |                |       |                      |
|---------------|----------------|-------|----------------------|
| Delivery mode | Taught/ Campus | Other | <input type="text"/> |
| Delivery term |                | Other | Terms 2 and 3        |

Ownership

|                     |         |
|---------------------|---------|
| Primary department  | Physics |
| Additional teaching | None    |

departments

Delivery campus **South Kensington**

### Collaborative delivery

Collaborative delivery? **N**

External institution **N/A**  
External department **N/A**  
External campus **N/A**

### Associated staff

| Role                 | CID | Given name      | Surname          |
|----------------------|-----|-----------------|------------------|
| <b>Module Leader</b> |     | <b>Jonathan</b> | <b>Halliwell</b> |
|                      |     |                 |                  |
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|                      |     |                 |                  |

### Learning and teaching

#### Module description

|                                |   |
|--------------------------------|---|
| Learning outcomes              | On completion of this module, you will be able to: <ul style="list-style-type: none"><li>• Interpret, work with and apply the concepts of real numbers, counting and infinity</li><li>• Make appropriate use of the rigorous definition of limits of sequences.</li><li>• Make use of series, functions, limits, continuity and be able to describe the basis of Calculus</li><li>• Interpret the Taylor series, and describe the sense in which it is an approximation in physics.</li></ul>   |
| Module content                 | <ul style="list-style-type: none"><li>• Sets and maps: Sets, notation, methods of proof, Russell's paradox, maps</li><li>• Numbers: Real numbers as infinite decimals, completeness of the reals, cardinality and countability, Cantor's 'diagonal' proof.</li><li>• Sequences: Convergence using <math>\epsilon-N</math>. Monotone and bounded sequences, sub-sequences, Bolzano-Weierstrass theorem. Cauchy sequences as convergent sequences.</li><li>• Series: Convergence of a series, comparison test, Cauchy and other standard tests (eg. root, ratio, alternating). Power series. Riemann reordering.</li><li>• Functions: Limits and continuity using <math>\epsilon-\delta</math>. Differentiable and smooth functions. Taylor's theorem and analytic functions.</li></ul> |
| Learning and Teaching Approach | Students will be taught using a combination of lectures, small-group tutorial teaching, office hours and directed exercises.  |
| Assessment Strategy            | An exam in term 3 covering all learning outcomes will comprise the main part of the summative assessment and will contribute 100% of the module mark.   |
| Feedback                       | Formative feedback will be provided orally within small-group tutorial classes. General feedback on written examinations for each module is provided in the form of written reports from the examiners for the students.  |
| Reading list                   | The module is self-contained and no additional books are required to be purchased by the students. Further discussion of material covered by the module, along with relevant problems can be found in: <ul style="list-style-type: none"><li>• K.E.Hirst, Numbers, Sequences and Series (London, Edward Arnold, 1995).</li><li>• G.Smith, Introductory Mathematics: Algebra and Analysis (Springer, 1998).</li><li>• M.Liebeck, A Concise Introduction to Pure Mathematics (Chapman and Hall, CRC, 2000).</li><li>• K.G. Binmore, Mathematical Analysis. A Straightforward Approach (Cambridge University Press, 1982).</li></ul>   |

### Quality assurance

### Office use only

Date of first approval

QA Lead

Date of last revision   
Date of this approval

Department staff   
Date of collection

Module leader

Date exported   
Date imported

Notes/ comments

## Programme structure

### Associated modules

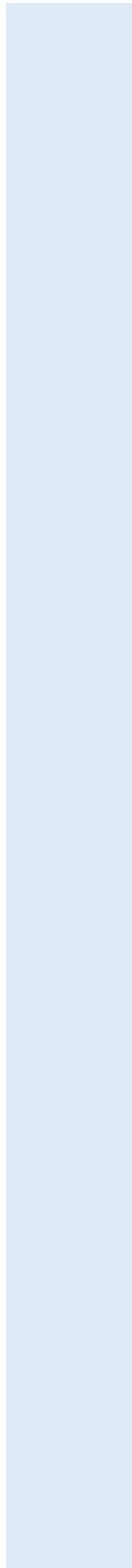
| UID | Legacy code | Module title | Requisite type |
|-----|-------------|--------------|----------------|
|-----|-------------|--------------|----------------|



# Programme structure

## Associated programmes

| UID | Legacy code | Programme title | Core? |
|-----|-------------|-----------------|-------|
|-----|-------------|-----------------|-------|



## Assessment details

|                |         |           |     |
|----------------|---------|-----------|-----|
| Grading method | Numeric | Pass mark | 40% |
|----------------|---------|-----------|-----|

## Assessments

| Assessment type | Assessment description | Weighting | Pass mark | Must pass? |
|-----------------|------------------------|-----------|-----------|------------|
|                 |                        |           | 40%       |            |
| Examination     | 2-hour exam            | 100%      | 40% N     |            |

100%